

# Is Inflation Default? The Role of Information in Debt Crises

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# Obs 1: Sovereign Debt and Having Your Currency

- Countries that borrow in their own currency more resilient to debt crises
  - ▶ High-debt countries: Japan vs. Italy
  - ▶ High-deficit countries: UK vs. Spain Plot
- “Domestic”-currency government bond prices react less to bad news

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  - ⇒ Interest rates do not jump in anticipation of default
- ...but printing money will cause inflation
  - ⇒ Interest rates should jump in anticipation of inflation

## Obs 2: Sovereign Spreads vs. Inflation

- Sovereign spreads move very fast, onset of rollover crises is sudden
- Inflation adjusts more slowly (at least in developed economies)

# Our Story

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- With foreign-currency debt, anticipate spike in default spreads  
⇒ coordination among **bondholders**
- With domestic-currency debt, anticipate escalation of inflation expectations  
⇒ coordination among **price setters**
- Price setters less precisely informed about gov't finances  
⇒ **Information frictions** underlie differential response of bond prices to shocks

# Roadmap

- Stylized macro model
- Show it maps into a two-period Bayesian trading game
  - ▶ repeated version of Albagli Hellwig Tsyvinski (2015)
- Comparative statics wrt relevant information precision



# Setup and Agents

- Three periods:  $t = 1, 2, 3$
- Government (described by a mechanical rule)
  - ▶ issues debt in  $t = 1$
  - ▶ repays (or not) in  $t = 3$ , depending on fiscal shock  $s$

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- Consequences of fiscal distress
  - ▶ Euro/foreign currency debt: (explicit) default via haircut
  - ▶ Yen/domestic currency debt: (implicit) default via inflation

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- Consequences of fiscal distress
  - ▶ Euro/foreign currency debt: (explicit) default via haircut
  - ▶ Yen/domestic currency debt: (implicit) default via inflation
- A continuum of two types of agents: “bond traders” and “workers”
  - ▶ risk neutral, unit wealth, cannot short assets, outside option = stay put

# Timing and Actions – First Period

- Government auctions debt at price  $q_1$ , promised repayment  $\hat{s}(q_1)$ ;  
Examples:
  - ▶ Eaton and Gersowitz (1981):  $\hat{s}(q_1) \equiv \hat{s}$
  - ▶ Calvo (1988):  $\hat{s}(q_1) \equiv \hat{s}/q_1$
- Bond traders
  - ▶ buy bonds conditional on price  $q_1$  (or stay put)
  - ▶ info on  $s$ : prior  $N(\mu_0, 1/\alpha_0)$ , private signal  $x_{i,1} \sim N(s, 1/\beta_1)$
- Residual noise-traders demand  $\Phi(\epsilon_1)$ , with  $\epsilon_1 \sim N(0, 1/\psi_1)$

# Timing and Actions – Second Period

- Bond traders must offload bonds
  - ▶ to new bond traders (€), or to workers through cash (¥)
- New bond traders (or workers)
  - ▶ buy bonds (cash) conditional on price  $q_2$  (or stay put)
  - ▶ info on  $s$ : prior  $N(\mu_0, 1/\alpha_0)$ , private signal  $x_{i,2} \sim N(s, 1/\beta_2)$
- Residual noise-agents demand  $\Phi(\epsilon_2)$ , with  $\epsilon_2 \sim N(0, 1/\psi_2)$

## Timing and Actions – Third Period

- If  $s \geq \hat{s}(q_1)$ , govt repays debt
- If  $s < \hat{s}(q_1)$ , **default** (or **inflation**)  $\Rightarrow$  **haircut** (or **currency debasement**)  $1 - \theta$

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Symmetries and key difference:

- Same eventual default/inflation payoff at the end ( $t = 3$ )
  - Same primary-market participants at the start ( $t = 1$ )
  - Identity of secondary-market ( $t = 2$ ) participants different:
    - ▶ **bond traders (€)** better informed than **workers (¥)**
- $\Rightarrow$   $\beta_2$  (or  $\psi_2$ ) **higher under €**

# Three Cases

- 1 No recall of past prices + exogenous default threshold  $\hat{s}$
- 2 Recall of past prices + exogenous default threshold  $\hat{s}$
- 3 Recall of past prices + endogenous default threshold  $\hat{s}(q_1)$



# The Simplest Case

Assume

- $\hat{s}(q_1) \equiv \hat{s}$  (constant)
- period-2 agents do not observe  $q_1$

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Period- $t$  agents' information set

- prior
- private signal  $x_{i,t}$
- can condition on current-period price  $\Rightarrow$  demand schedules  $d(x_{i,t}, q_t)$

## Period-2 Agents: Payoffs and Strategies

- Expected payoff

$$\underbrace{\theta \cdot \text{Prob}(s < \hat{s} | x_{i,2}, q_2) + 1 \cdot \text{Prob}(s \geq \hat{s} | x_{i,2}, q_2)}_{\substack{(\text{€}) \quad \mathbb{E}_{i,2}[\text{bond repayment}] \\ (\text{¥}) \quad \mathbb{E}_{i,2}[1/P_3]}} - \underbrace{q_2}_{\substack{\text{bond price} \\ 1/P_2}}$$

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- Posterior beliefs on  $s$  are FOSD-increasing in  $x_{i,2}$ 
  - Buy if signal is above threshold:

$$d(x_{i,2}, q_2) = \mathbb{1}[x_{i,2} \geq \hat{x}_2(q_2)]$$

## Period-2: Market Clearing and Beliefs

- Period-2 market clearing condition

$$\underbrace{\text{Prob}(x_{i,2} \geq \hat{x}_2(q_2)|s)}_{\text{informed nominal-asset demand}} = \underbrace{1 - \Phi(\epsilon_2)}_{\text{nominal-asset supply (net of noise agents)}}$$

- Market clearing implies

$$s + \frac{\epsilon_2}{\sqrt{\beta_2}} = \hat{x}_2(q_2)$$

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- Market clearing implies

$$z_2 := s + \frac{\epsilon_2}{\sqrt{\beta_2}} = \hat{x}_2(q_2)$$

- We focus on equilibria where  $z_t$  is informationally equivalent to  $q_t$
- Second-period agents posterior beliefs

$$s|x_2, z_2 \sim N\left(\frac{\alpha_0\mu_0 + \beta_2x_2 + \beta_2\psi_2z_2}{\alpha_0 + \beta_2(1 + \psi_2)}, \frac{1}{\alpha_0 + \beta_2(1 + \psi_2)}\right)$$

## Period-2: Equilibrium

- Marginal agent's indifference condition

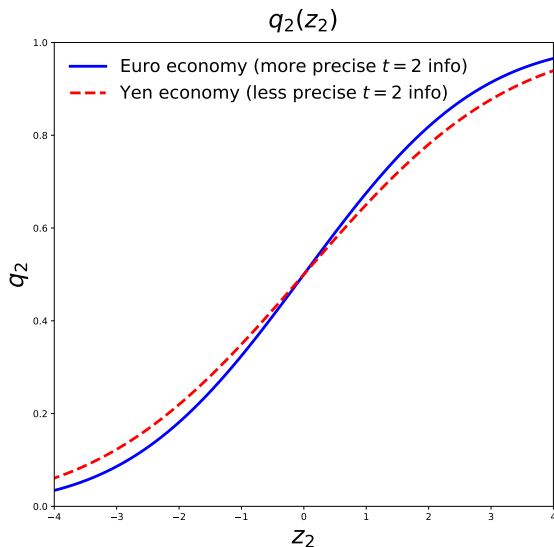
$$\theta + (1 - \theta)\text{Prob}(s \geq \hat{s} | x_{i,2} = \hat{x}_2(q_2), q_2) = q_2$$

- Equilibrium  $t = 2$  price

$$q_2(z_2) = \theta + (1 - \theta)\Phi\left(\frac{(1 - w_S)\mu_0 + w_S z_2 - \hat{s}}{\sigma_S}\right)$$

$$w_S := \frac{\beta_2(1+\psi_2)}{\alpha_0 + \beta_2(1+\psi_2)}, \quad \sigma_S^2 := \frac{1}{\alpha_0 + \beta_2(1+\psi_2)}$$

# Comparative Statics (more precise info = higher $\beta_2$ or $\psi_2$ )





## Period-1: Strategies and Beliefs

- Expected payoff

$$\mathbb{E}[q_2(z_2)|x_{i,1}, q_1] - q_1$$

- Monotone threshold strategies again
- Market clearing implies

$$z_1 := s + \epsilon_1 / \sqrt{\beta_1} = \hat{x}_1(q_1)$$

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- Market clearing implies

$$z_1 := s + \epsilon_1 / \sqrt{\beta_1} = \hat{x}_1(q_1)$$

- First-period agents posterior beliefs on  $z_2$ , not just  $s$

$$z_2|(z_1, x_1) \sim N\left(\frac{\alpha_0\mu_0 + \beta_1x_1 + \beta_1\psi_1z_1}{\gamma_1}, \frac{1}{\gamma_1} + \frac{1}{\psi_2\beta_2}\right)$$

$\gamma_1$

## Period-1: Equilibrium

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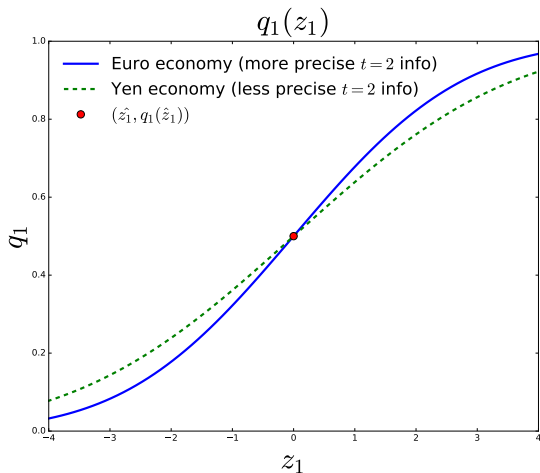
- Equilibrium  $t = 1$  price

$$q_1(z_1) = \theta + (1 - \theta)\Phi \left[ \frac{\mu_0 - \hat{s}}{\sqrt{w_S^2 \sigma_{S|B}^2 + \sigma_S^2}} + \frac{w_S w_B}{\sqrt{w_S^2 \sigma_{S|B}^2 + \sigma_S^2}} (z_1 - \mu_0) \right]$$

$$w_B := \frac{\beta_1(1+\psi_1)}{\alpha_0 + \beta_1(1+\psi_1)}, \quad \sigma_{S|B}^2 := \frac{1}{\gamma_1} + \frac{1}{\psi_2\beta_2}$$

$q_1$  with recall

# Comparative Statics (more precise info = higher $\beta_2$ or $\psi_2$ )



Propositions 1&2

# What if there is Recall of the First-Period Price?

- Same payoffs, different information set for period-2 agents
- $q_1$  new source of common knowledge with period-1 traders
- $q_1 \iff z_1$
- Marginal period-1 trader and period-2 trader have different weight on  $z_1$ ; period-2 information is **not** finer than period 1
- Difference breaks law of iterated expectations:

$$q_1 = E[E[\pi(\theta)|\mathcal{I}_2]|\mathcal{I}_1]$$

- Second-period agents posterior beliefs

$$s|x_2, z_2, z_1 \sim N\left(\frac{\alpha_0\mu_0 + \beta_1\psi_1z_1 + \beta_2x_2 + \beta_2\psi_2z_2}{\alpha_0 + \beta_1\psi_1 + \beta_2(1 + \psi_2)}, \sigma_S^2 := \frac{1}{\alpha_0 + \beta_1\psi_1 + \beta_2(1 + \psi_2)}\right)$$

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- Equilibrium  $t = 1$  price

$$q_1(z_1) = \theta + (1 - \theta)\Phi\left[\frac{\mu_0 - \hat{s}}{\sqrt{w_{2,S}^2\sigma_{S|B}^2 + \sigma_S^2}} + \frac{(w_{1,S} + w_{2,S}w_B)}{\sqrt{w_{2,S}^2\sigma_{S|B}^2 + \sigma_S^2}}(z_1 - \hat{s})\right]$$

$q_1$  w/out recall

$w_{1,S}, w_{2,S}$

$\gamma_1$



## Comparative Statics: Some Intuition

$$q_1(z_1) = \theta + (1 - \theta)\Phi \left[ \frac{\mu_0 - \hat{s}}{S} + K(z_1 - \mu_0) \right]$$

$$K := \frac{(w_{1,S} + w_{2,S}w_B)}{\sqrt{w_{2,S}^2 \left( \frac{1}{\gamma_1} + \frac{1}{\beta_2\psi_2} \right) + \sigma_S^2}}$$

- Always get single crossing, as before
- Direction of crossing dictated by  $K$

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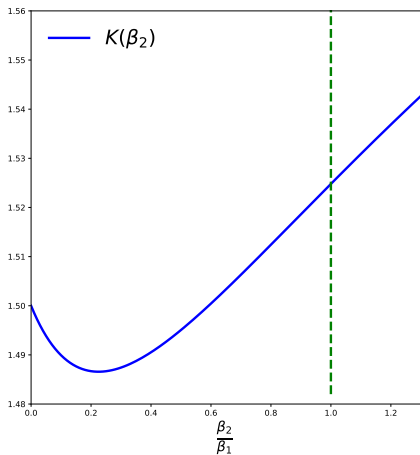
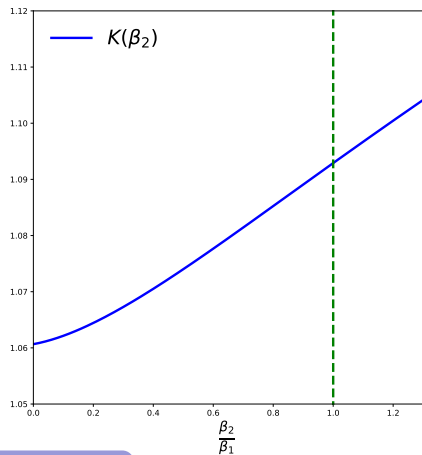
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- Always get single crossing, as before
- Direction of crossing dictated by  $K$
- Effect of  $\beta_2, \psi_2$  on  $K$  more involved:
  - ▶  $\beta_2 \uparrow \implies$  period-2 agents give less weight to prior, but also to  $q_1$
  - ▶ Less weight on prior  $\implies q_2$  tracks  $s$  better
  - ▶ Less weight on  $q_1 \implies q_2$  tracks  $s$  better, but potentially less correlated with  $q_1$ , ambiguous

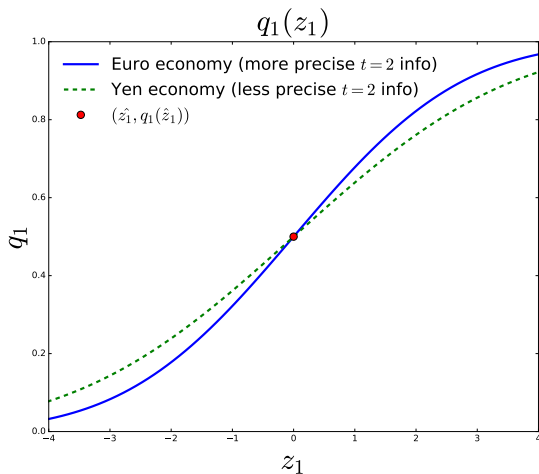
# Comparative Statics

$$K := \frac{(w_{1,S} + w_{2,S}w_B)}{\sqrt{w_{2,S}^2\sigma_{S|B}^2 + \sigma_S^2}}$$



Propositions 3&4

# Single Crossing Again



# Endogenous Default Threshold: Equilibrium

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- Consider endogenous default cutoff: gov't repays iff  $s \geq \hat{s}(q_1)$
- Period-1 price only implicitly characterized, solves

$$q_1 = \theta + (1 - \theta)\Phi \left[ \frac{\mu_0 - \hat{s}(q_1)}{\sqrt{w_{2,S}^2 \sigma_{S|B}^2 + \sigma_S^2}} + \frac{(w_{1,S} + w_{2,S} w_B)}{\sqrt{w_{2,S}^2 \sigma_{S|B}^2 + \sigma_S^2}} (z_1 - \mu_0) \right]$$

# Endogenous Default Threshold: Comparative Statics

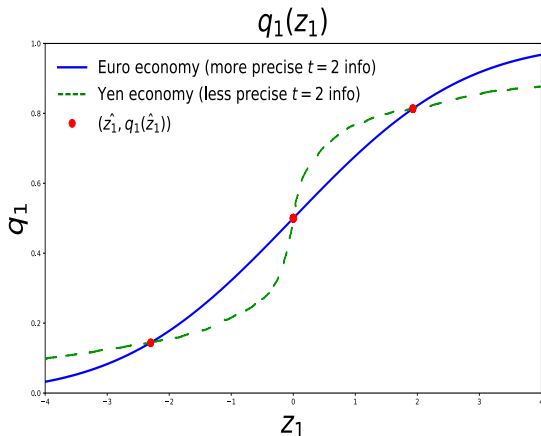
## Comparative statics

- on  $\psi_2$ : still valid, single crossing

# Endogenous Default Threshold: Comparative Statics

## Comparative statics

- on  $\psi_2$ : still valid, single crossing
- on  $\beta_2$ : price changes are still the same in tail events





# Conclusion

- Heterogeneity of information has important implications for debt management
- We have shown insurance role of domestic-currency debt
- Next step: optimal theory of currency denomination (study of effects on ex ante price)

# Thank You!

# The “Original Sin”

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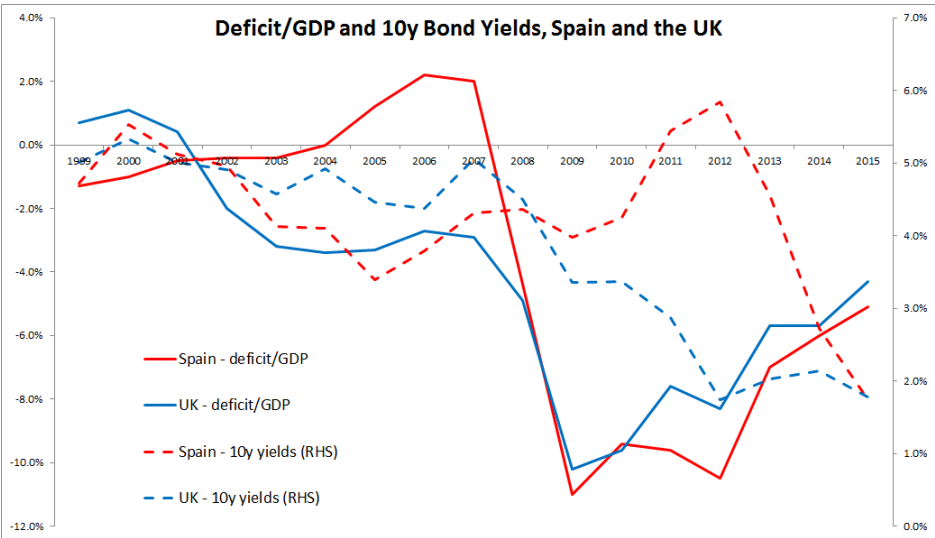
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- If this were the problem, we would expect interest rates to be *more* sensitive to bad news with domestic-currency debt
- Bordo-Meissner (2006): Currency mismatch not necessarily associated with more frequent crises
- Ability to devalue and mitigate recession not always relevant (in the 2008 crisis the yen appreciated)

## Deficit/GDP and 10y Bond Yields, Spain and the UK



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# Macro Model: Setup and actors

- Three periods
- Bond traders: strategic and noise
- Workers: strategic and noise
- Government (described by a mechanical rule)

[back to setup](#)



# Workers: Preferences and Technology

- Only alive in periods 2 and 3
- Strategic workers
  - ▶ One unit of endowment in period 2
  - ▶ Wish to consume in period 3, risk neutral
  - ▶ Can store good (zero return) or sell it
- Noise workers
  - ▶ (Unobserved) relative mass  $\Phi(\epsilon_2^w)$ ,  $\epsilon_2^w \sim N(0, 1/\psi_2^w)$
  - ▶ Can produce in period 3
  - ▶ Demand 1 unit of consumption in period 2

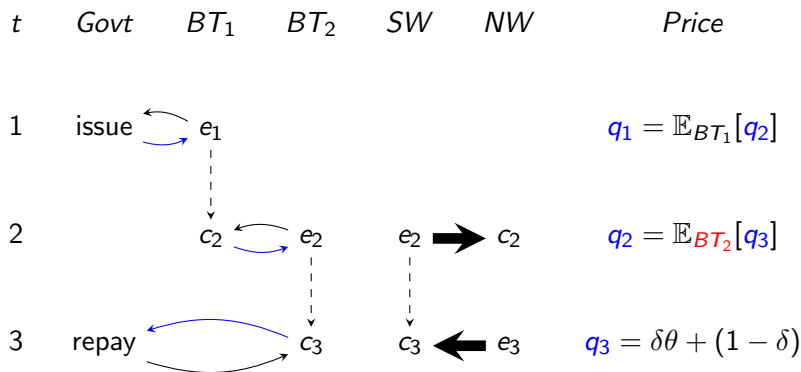
# Bond Traders: Preferences and Technology

- 2 OLGs living for two periods
- Endowed with goods when young
- Want to consume when old, risk neutral
  
- Strategic traders:
  - ▶ Can store
  - ▶ Can buy one unit of government bonds
  
- Noise traders:
  - ▶ Demand an (unobserved) fraction  $\Phi(\epsilon_t^b)$ ,  $\epsilon_t^b \sim N(0, 1/\psi_t^b)$ , of gov't debt
  
- Mass of bond traders negligible compared to workers

## Government - “Euro” scenario

- Auctions one unit of debt in period 1 (per capita per young strategic trader), price  $q_1$
- Debt is a promise to pay  $\hat{s}(q_1)$  Euros (goods) in period 3. Examples:
  - ▶  $\hat{s}(q_1) \equiv 1$  (Eaton and Gersovitz)
  - ▶  $\hat{s}(q_1) \equiv 1/q_1$  (Calvo)
- In period 3, gov't collects taxes, depending on the realization of  $s \sim N(\mu_0, 1/\alpha_0)$ :
  - ▶ If  $s \geq \hat{s}(q_1)$ , full repayment
  - ▶ Otherwise, haircut  $1 - \theta$ , gov't pays back  $\theta\hat{s}(q_1)$

# Euro Markets



goods; *bonds*; storage (dashed)

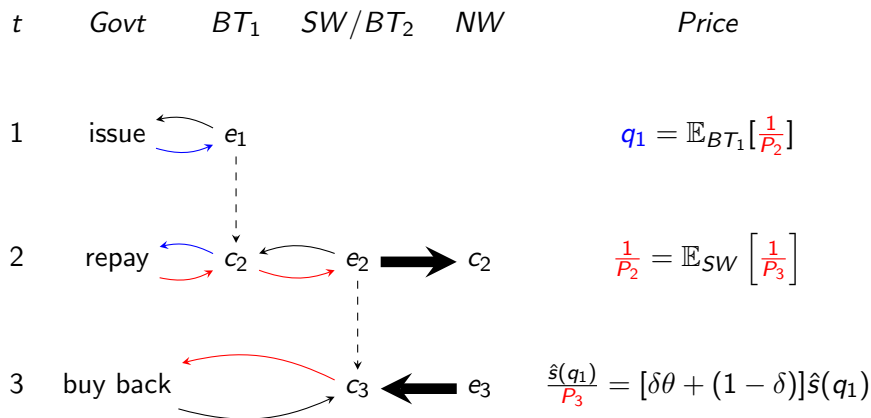
Yen Markets

## Government - “Yen” scenario

- Auctions one unit of debt in period 1 (per capita per young strategic trader), price  $q_1$
- Debt is a promise to pay  $\hat{s}(q_1)$  Yen.
- In period 2, gov't prints Yen, pays debt back.
- In period 3, gov't collects taxes, depending on the realization of  $s \sim N(\mu_0, 1/\alpha_0)$ :
  - If  $s \geq \hat{s}(q_1)$ , collects  $\hat{s}(q_1)$
  - Otherwise, collects  $\theta\hat{s}(q_1)$ } (same as Euro scenario)
- Period-3 taxes used to buy Yen back. Price level is either 1 or  $1/\theta$ .

Price Level Determination

# Yen Markets



goods; *bonds*; *cash*; storage (dashed)

Euro Markets

# Euro vs. Yen: the Key Difference

- Eventual default/inflation is the same at the end ( $t = 3$ )
- Identity of primary-market participants is the same at the start ( $t = 1$ )
- **Period 2** Identity of secondary-market participants different:
  - ▶ Under Euro, bonds offloaded to **new bond traders**
  - ▶ Under Yen, bonds offloaded to **workers (through cash)**
- With same information, same prices/payoffs in the 2 scenarios:
  - ▶ collapse them into a single problem:  $q_2 := 1/P_2$  in the Yen case
  - ▶ index scenarios with period-2 agents' information precision

# Price Level Determination, Yen Economy

Government money valuation equation

$$\frac{M}{P_3} = \text{real tax revenues}$$

and since  $M = \hat{s}(q_1)$  (govt repays debt with money at  $t = 2$ )

$$\frac{M}{P_3} = \frac{\hat{s}(q_1)}{P_3} = \delta \cdot \theta \hat{s}(q_1) + (1 - \delta) \cdot \hat{s}(q_1)$$

so that

$$\begin{cases} \delta = 1 & P_3 = 1/\theta \\ \delta = 0 & P_3 = 1 \end{cases}$$

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# Equilibrium Definition

## Definition

A Perfect Bayesian Equilibrium consists of bidding strategies  $d(x_{i,t}, q_t)$  for strategic players, a price function  $q(s, \epsilon_t)$  and posterior beliefs  $p(x_{i,t}, q_t)$  such that

- (i)  $d(x_{i,t}, q_t)$  is optimal given beliefs  $p(x_{i,t}, q_t)$ ,
- (ii)  $q(s, \epsilon_t)$  clears the market for all  $(s, \epsilon_t)$ , and
- (iii)  $p(x_{i,t}, q_t)$  satisfies Bayes' Law for all market clearing prices  $q_t$ .

## More Definitions

- Precision of first-period posterior beliefs

$$\frac{1}{\gamma_1} := \frac{1}{\alpha_0 + \beta_1(1 + \psi_1)}$$

Case 1:  $t = 1$  beliefs

Case 1: comparative statics

- Second-period Bayesian weights (case with recall)

$$w_{1,S} := \frac{\beta_1 \psi_1}{\alpha_0 + \beta_1 \psi_1 + \beta_2(1 + \psi_2)} \quad w_{2,S} := \frac{\beta_2(1 + \psi_2)}{\alpha_0 + \beta_1 \psi_1 + \beta_2(1 + \psi_2)}$$

Case 2:  $q_1$

- Aggregate noise term of first-period price (case with recall)

$$S := \sqrt{w_{2,S}^2 \left( \frac{1}{\gamma_1} + \frac{1}{\beta_2 \psi_2} \right) + \sigma_S^2}$$

Case 2:  $q_1$

Case 2: comparative statics

# Simplest Case

## Proposition (1)

*There exists a cutoff level  $\hat{z}_1^\beta \in \mathbb{R}$  such that when  $z_1 < \hat{z}_1^\beta$ , a decrease in  $\beta_2$  improves the issuance price  $q_1$ , whereas the reverse occurs for  $z_1 > \hat{z}_1^\beta$ .*

## Proposition (2)

*There exists a cutoff level  $\hat{z}_1^\psi \in \mathbb{R}$  such that when  $z_1 < \hat{z}_1^\psi$ , a decrease in  $\psi_2$  improves the issuance price  $q_1$ , whereas the reverse occurs for  $z_1 > \hat{z}_1^\psi$ .*

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# With Recall, Exogenous Threshold

## Proposition (3)

*There exists a cutoff level  $\hat{z}_1^\psi \in \mathbb{R}$  such that when  $z_1 < \hat{z}_1^\psi$ , a decrease in  $\psi_2$  improves the issuance price  $q_1$ , whereas the reverse occurs for  $z_1 > \hat{z}_1^\psi$ .*

## Proposition (4)

*Assume that  $\psi_2 \geq \psi_1$  and  $\beta_2^A \geq \beta_1$ . Let  $\beta_2^B < \beta_2^A$ . Then there exists a cutoff level  $\hat{z}_1^\beta \in \mathbb{R}$  such that when  $z_1 < \hat{z}_1^\beta$ ,  $q_1$  evaluated at  $\beta_2^A$  is smaller than at  $\beta_2^B$ , whereas the reverse occurs for  $z_1 > \hat{z}_1^\beta$ , holding all other parameters fixed.*

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# With Recall, Endogenous Threshold

## Proposition (5)

*Assume that  $\psi_2 \geq \psi_1$  and  $\beta_2^A \geq \beta_1$ , and let the conditions for equilibrium uniqueness hold. Let  $\beta_2^B < \beta_2^A$ . Then there exist two cutoffs level  $\hat{z}_1^L \leq \hat{z}_1^H \in \mathbb{R}$  such that when  $z_1 < \hat{z}_1^L$ ,  $q_1$  evaluated at  $\beta_2^A$  is smaller than at  $\beta_2^B$ , whereas the reverse occurs for  $z_1 > \hat{z}_1^H$ , holding all other parameters fixed.*